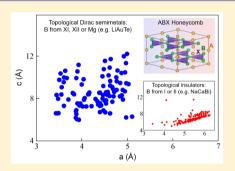


# Topological Insulators versus Topological Dirac Semimetals in **Honeycomb Compounds**

Xiuwen Zhang,\*,<sup>†,‡,</sup>∥<sub>0</sub> Qihang Liu,<sup>‡,||,∇</sup><sub>0</sub> Qiunan Xu,<sup>§,||</sup> Xi Dai,<sup>⊥</sup> and Alex Zunger\*,<sup>‡</sup>

Supporting Information

ABSTRACT: Intriguing physical properties of materials stem from their chemical constituents, whereas the connection between them is often not clear. Here, we uncover a general chemical classification for the two quantum phases in the honeycomb ABX structure—topological insulator (TI) and topological Dirac semimetal (TDSM). First, we find among the 816 (existing as well as hypothetical) calculated compounds, 160 TIs (none were noted before), 96 TDSMs, 282 normal insulators (NIs), and 278 metals. Second, based on this classification, we have distilled a simple chemical regularity based on compound formulas for the selectivity between TI and TDSM: the ABX compounds that are TDSM have B atoms (part of the BX honeycomb layers) that come from the periodic table columns XI (Cu, Ag, Au) or XII (Zn, Cd, Hg), or Mg (group II), whereas the ABX compounds whose B atoms come from columns I (Li, Na, K, Rb, Cs) or II (Ca, Sr,



Ba) are TIs. Third, focusing on the ABX bismide compounds that are thermodynamically stable, we find a structural motif that delivers topological insulation and stability at the same time. This study opens the way to simultaneously design new topological materials based on the compositional rules indicated here.

## 1. INTRODUCTION

Topological insulators (TIs)<sup>1-4</sup> and topological Dirac semimetals (TDSMs)<sup>5,6</sup> are two classes of quantum phases, both having in their bulk band structures an inverted order of the occupied valence and unoccupied conduction bands at the time-reversal invariant momenta (TRIM) in the Brillouin zone (BZ). In three-dimensional TI compounds (e.g., Bi<sub>2</sub>Se<sub>3</sub>), such bulk band inversion is characterized by a topological invariant,<sup>3</sup>  $Z_2 = 1$ , and leads to the appearance at the bulk-terminated surface of linearly dispersed ("massless") and mutually crossing ("metallic") energy bands, a construction referred to as surface Dirac cones.<sup>8</sup> In three-dimensional TDSM compounds (e.g., Na<sub>3</sub>Bi<sup>5</sup>), on the other hand, band inversion is characterized by a two-dimensional topological invariant,  $\nu_{2D} = 1$ , and leads to the appearance of Dirac cones already in the bulk, a construction protected by crystalline symmetries.<sup>5,10</sup> Note that TDSM is distinct from nontopological DSM such as the hypothetical BiO<sub>2</sub> compound in the cristobalite structure, where a topological invariant cannot be defined. 11 The existence of a given compound as TI or TDSM depends sensitively on structure and composition and is a rather consequential distinction because these two quantum phases have very different physical properties (e.g., quantum spin Hall effect4 in CdTe/HgTe quantum well TI versus giant magnetoresistance<sup>12</sup> in Na<sub>3</sub>Bi TDSM) and different potential applications. However, one is hard pressed to guess based on structure and composition alone which compound will be nontopological and which will be topological and, for the latter, which will be a TI and which will be TDSM. We address this question via direct calculations of the topological invariants for many compositions within the context of a given structure—the honeycomb lattice—and uncover intriguing chemical regularities.

The ABX honeycomb structure (ZrBeSi-type, space group P6<sub>3</sub>/mmc; No. 194) consists of BX planar honeycomb layers and "stuffing" A layers between these layers. Our interest in the honeycomb lattice stems from a few reasons: (i) A closer inspection (see below) of the predicted TIs in groups I-XI-VI (such as LiAuTe<sup>13</sup>) and I-XII-V (such as LiHgSb<sup>13</sup>) honeycomb compounds reveals that they are in fact all TDSMs. Other previously assigned topological materials in groups XI-II-V (such as AgBaBi<sup>14,15</sup>) are also established to be TDSMs. Thus, at this point there are no material realizations of TI in ABX honeycomb compounds. (ii) The special crystalline symmetries in the honeycomb ABX structure

Received: June 24, 2018 Published: September 26, 2018

<sup>&</sup>lt;sup>†</sup>Shenzhen Key Laboratory of Flexible Memory Materials and Devices, College of Electronic Science and Technology, Shenzhen University, Guangdong 518060, China

<sup>&</sup>lt;sup>‡</sup>Renewable and Sustainable Energy Institute, University of Colorado, Boulder, Colorado 80309, United States

<sup>§</sup>Beijing National Laboratory for Condensed Matter Physics, and Institute of Physics, Chinese Academy of Sciences, Beijing 100190,

 $<sup>^\</sup>perp$ Department of Physics, The Hong Kong University of Science and Technology, Clear Water Bay, Hong Kong

Journal of the American Chemical Society

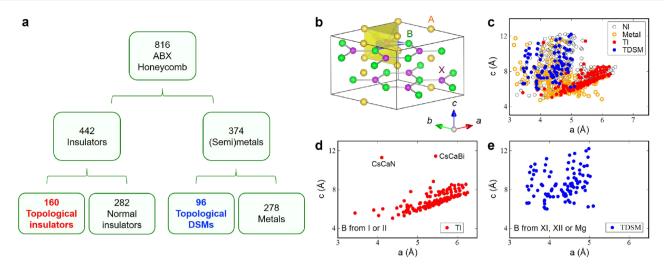


Figure 1. Classification of honeycomb ABX compounds in eight chemical groups: I-II-V, I-XII-V, XI-II-V, XI-XII-V, I-I-VI, I-XII-V, XI-II-V, XI-II-V,

offer the opportunity to realize a variety of interesting physical properties even beyond TI and TDSM, such as hidden spin polarization<sup>16</sup> and hourglass Fermion.<sup>17</sup> (iii) There are ~800 (real as well as hypothetical) compounds in this group, providing a diverse range of chemical bonding, so the conclusions drawn are likely to be rather general. In this study, we performed high-throughput calculation of the ~800 octet ABX compounds (see Figure S1 in the Supporting Information). Whereas most of the ABX compounds in Figure S1 do not adopt the honeycomb structure (compounds indicated in Figure S1 in red color are stable in the honeycomb structure; others have different structures), we have considered in the first step of this calculation all compounds in the honeycomb structure so as to establish the particular structural motif (section 2.2) that makes some compounds TI and others TDSM. In the second step (section 2.3), we establish for a subset of compounds that are the most interesting the lowestenergy structure. From the above calculations, a simple chemical regularity based on compound formulas for the selectivity between TI and TDSM is distilled. This opens the way to design topological materials with intriguing physical properties from the basis of chemical constituents. It also shed light on the correlation between topological properties and local structural motifs, suggesting design of TIs using local motifs as building blocks.

#### 2. RESULTS AND DISCUSSION

**2.1. Search of Topological Materials from 816 ABX Honeycomb Compounds.** Looking first for atomic sequences A/B/X at the fixed crystal structure, we have performed high-throughput density functional theory (DFT) and topological invariant calculations on 816 real plus hypothetical honeycomb ABX compositions (Figure 1a), sorting them into topological (TIs or TDSMs) versus trivial (normal insulators or metals). Our first-principles calculations show that the 816 honeycomb compounds are divided into 442 insulators plus 374 metals + semimetals. The latter are divided into 96 topological Dirac semimetals plus 278 ordinary

metals, whereas the 442 insulators are divided into 160 TIs plus 282 normal insulators ( $Z_2 = 0$  but could have nonsymmorphic symmetry-protected hourglass Fermion-like surface states such as in KHgSb<sup>17</sup>). We then identify within the first group of 256 topological compounds 160 TIs and 96 TDSMs by examining if the irreducible representations of the inverted bands are the same (implying band anticrossing, hence TI) or different (implying band crossing, hence TDSM). The significant number of newly recognized TIs in this group, as summarized in Figure 1a, is noteworthy, but none overlaps with those initially predicted to be TI based on a restricted view of the BZ. 13 Based on this classification, we have distilled a simple chemical regularity for the selectivity between TI and TDSM: The ABX compounds that are TDSM have B atoms (part of the BX honeycomb layers) that come from the periodic table columns XI (Cu, Ag, Au) or XII (Zn, Cd, Hg), or Mg (group II), whereas the ABX compounds whose B atoms comes from columns I (Li, Na, K, Rb, Cs) or II (Ca, Sr, Ba) are TIs.

2.2. Separation of Topological Materials into TIs and **TDSMs.** We have performed DFT calculations with spin-orbit coupling (SOC) of electronic structures and topological invariants (see section I in the Supporting Information for the electronic structures 18-23 and evaluation methods for topological invariants<sup>9,24-26</sup>) of the ABX honeycomb structures (see Figure 1). We are aware of the DFT errors on evaluating the band gaps of insulators and semiconductors that could affect the prediction of topological materials from DFT, and we test the DFT results by comparing them with HSE<sup>23</sup> calculations (see section II.B in the Supporting Information which shows that one out of four DFT-predicted topological materials becomes a normal insulator according to HSE calculations). On the other hand, the separation of topological materials into TIs and TDSMs, concerning the band-crossing/ band-anticrossing of band-inverted compounds, is not affected by the DFT errors on band gaps. We find that including SOC in structural relaxation has negligible effect on band-edge electronic states (see section II.C in the Supporting

Journal of the American Chemical Society

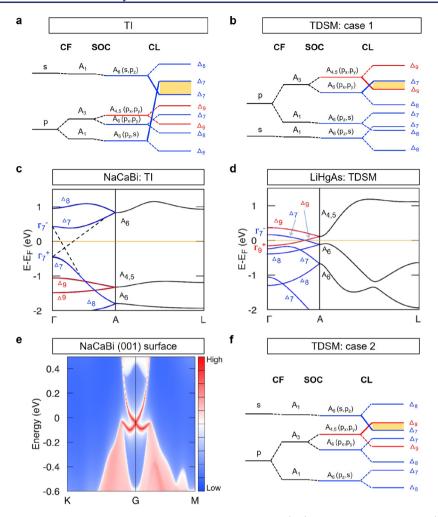


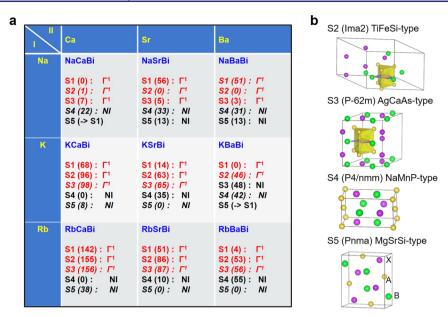
Figure 2. Electronic structures of TI and TDSM phases in honeycomb ABX structures. (a,b) Energy level diagrams for (a) TI with s above p state mainly from X atoms and (b) TDSM with s below p state showing the effect of crystal field splitting, SOC, and coupling between B–X layers (CL) on the states around the Fermi level.  $A_1$  and  $A_3$  ( $A_{4,5}$  and  $A_6$ ) are the irreducible representations at A point in the Brillouin zone in the absence (appearance) of SOC, and  $\Delta_7$ ,  $\Delta_8$ , and  $\Delta_9$  are those on the Γ–A line with SOC. The shaded areas indicate the inverted gap near the center of BZ. (c,d) Band structures of (c) NaCaBi (TI) and (d) LiHgAs (TDSM) with SOC.  $\Gamma^+_{7,7}$  f<sup>-</sup><sub>7</sub>, etc. are the irreducible representations at Γ point. Red and blue bands denotes  $\Delta_9 + \Delta_9$  and  $\Delta_7 + \Delta_8$  band character, respectively. We use  $A_{4,5}$  as an abbreviation of  $A_4 + A_5$ . The dashed lines in panel (c) are a guide for the eyes for the band inversion. (e) The (001) surface states of NaCaBi calculated by the effective tight-binding Hamiltonians of a freestanding thick slab consisting of 20 unit cells along the (001) direction. The color scale indicates the relative density of surface states. (f) Energy level diagrams for TDSM with s above p state.

Information). Thus, we perform structural relaxation without SOC, followed by electronic structure calculation with SOC that could increase band inversion energies in topological materials. In the honeycomb ABX lattice shown in Figure 1b, the positions of the atoms are T(A) = (0,0,0); T(B) = (1/3,2/3,1/4); T(X) = (2/3,1/3,1/4). Note that the B atom has as first and second shell neighbors  $X_3A_6$ , and the X atom has neighbors  $B_3A_6$ , whereas the A atom has as neighbors  $[X_6B_6]A_6$  or  $A_6[X_6B_6]$  (X and B are at equal distance) depending on the lattice constants.

The topological invariants were calculated from band parities  $^{27}$  for the centrosymmetric honeycomb ( $P6_3/mmc$ ) structure, with structural parameters obtained by total energy and force minimization (see section I in the Supporting Information for theoretical methods). The classification of the 816 compounds into TI, TDSM, normal insulator, and metals is given in Figure 1a and summarized graphically in terms of the lattice parameters a and c in Figure 1c—e (see Figure S1 in the Supporting Information for the classified list of the 816

compounds). We emphasize that, although these structures are locally stable, there is no assurance that they are stable with respect to alternative structures or relative to phase separation into constituent phases. We nevertheless include all of them at this stage to clarify how the electronic feature of TI-ness or TDSM-ness emerges from a given composition at fixed structure. Filtering out stable structures will be discussed later for a subset of interesting compounds.

Figure 1 reveals a simple chemical regularity for the selectivity between TI and TDSM: The ABX compounds that are TDSM have B atoms (part of the BX honeycomb layers) that come from the periodic table columns XI (Cu, Ag, Au) or XII (Zn, Cd, Hg), or Mg (group II), whereas the ABX compounds whose B atoms comes from columns I (Li, Na, K, Rb, Cs) or II (Ca, Sr, Ba) are TIs. To understand this, we will analyze next the origin of TI versus TDSM in terms of symmetry (band crossing versus band anticrossing) and then connect these symmetries with geometrical factors such as c/a ratio controlling the crystal field splitting as well as the



**Figure 3.** Topological properties of the I–II–Bi group of ABX materials. (a) Topological (red) and nontopological (black) phases in I–II–Bi, with the crystal structures observed<sup>32</sup> for the compounds in this group (denoted S1–S5). Italic font indicates BAX configuration with cation swapping compared to ABX (we chose the lower-energy configuration from ABX and BAX). The total energies relative to the ground-state structure are given in parentheses (in meV/atom). (b) Crystal structures of the I–II–Bi group of materials. The honeycomb structure (S1) is shown in Figure 1b.

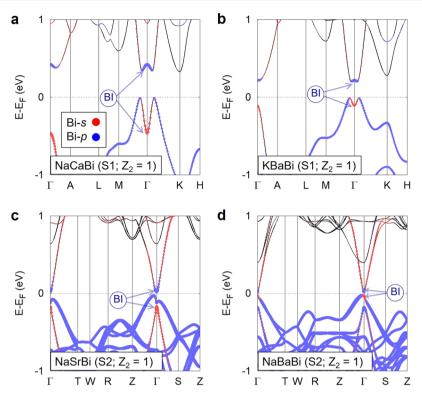
interaction between local structures and hence crossing versus anticrossing.

2.2.1. Band Crossing (TDSM) versus Band Anticrossing (TI). Both TI and TDSM phases have band inversion, but the group representations of the inverted bands could lead to either band crossing or anticrossing off the TRIM point. This results in TDSM or TI, respectively. Figure 2a,b explains schematically the orbital conditions for TI and TDSM, respectively, as further illustrated by actual band structure calculations for NaCaBi (a TI, Figure 2c) and LiHgAs (a TDSM, Figure 2d). This can be illustrated by considering the behavior along the  $\Gamma$ -A direction. With the presence of SOC, the bands at the A point are four-fold degenerate due to the nonsymmorphic symmetry operation of space group P6<sub>3</sub>/ mmc.<sup>28</sup> There are two types of group representations at the wavevector A:  $A_6$  and  $A_4 + A_5$  (see Table S2 in the Supporting Information). In the direction from A to  $\Delta$  (0, 0,  $\Delta$ ) the 4-fold degenerate states split into two two-fold bands  $A_6 \rightarrow \Delta_7 + \Delta_8$ and  $A_4 + A_5 \rightarrow \Delta_9 + \Delta_9$ . Therefore, the bands at  $\Delta$  have three possible double-group representations:  $\Delta_7$ ,  $\Delta_8$ , and  $\Delta_9$ . In the TI case, as found in our calculations (Figure 2a), the inverted gap consists of the occupied  $\Delta_7$  state, originating from A<sub>6</sub> and formerly a conduction (s) band, lying below the empty  $\Delta_7$ state originating also from A<sub>6</sub>, formerly a valence (p) band. When both inverted bands have the same  $\Delta_7$  representation, there must be band anticrossing, and thus the system will be a TI, as shown in Figure 2a and exemplified by NaCaBi in Figure 2c. It is also shown in Figure 2c that the two inverted  $\Delta_7$  states at  $\Delta$  become at  $\Gamma$  point  $\Gamma^+_7$  and  $\Gamma^-_7$ , respectively, with opposite parities as indicated by plus/minus signs (see Table S3 in the Supporting Information for their character table). The (001) surface states of NaCaBi with a clear Dirac cone are shown in Figure 2e, indicating a strong TI phase. In the TDSM case shown in Figure 2b and exemplified by LiHgAs in Figure 2d (indicating the parities of the inverted states  $\Gamma_7^-$  and  $\Gamma_9^+$  at  $\Gamma$ ), the former conduction s-band drops below the former valence p-band (see Figure 2b) due to the strong relativistic

Mass-Darwin effect of Hg, hybridizing with the pz state, leaving the upper braches of the  $p_{x,y}$ -bands as conduction bands. The inverted gap of LiHgAs is between the occupied  $\Delta_9$ state originating from  $A_{4,5}$  (an abbreviation for  $A_4 + A_5$ ) and the empty  $\Delta_7$  state originating from  $A_6$  of the former valence pband. Because these states originate from different (A<sub>4,5</sub> and A<sub>6</sub>) symmetries, they can cross, leading to TDSM. Figure 2f shows another case of the TDSM phase as found in our calculations (the band structure is exemplified by RbMgN in Figure S4 of the Supporting Information), in which the conduction s-band does not drop below the valence p-band, analogous to the TI case (Figure 2a). However, in Figure 2f, the upper-most state of the valence p-band is the  $\Delta_9$  state (versus the  $\Delta_7$  state in Figure 2a), and the inverted gap is between this  $\Delta_9$  state and the  $\Delta_7$  state originating from  $A_6$ (former conduction s-band). The two states with different irreducible representations cross, leading to TDSM. Thus, the simple design principle for TI versus TDSM classification of band-inverted compounds is whether the representations of the inverted bands are equal or different.

2.2.2. Geometrical Factors Controlling Crossing versus Anticrossing and Hence TDSM versus TI in the Honeycomb Structure. Whereas the crossing versus anticrossing (Figure 2c,d) explains the generic TDSM versus TI behavior, the understanding of which compounds and lattice constants fall into TDSM versus TI behavior requires a more detailed understanding of crystal field splitting, SOC, and coupling between B-X layers. This is explained in Figure 2a,b,f for the three types of TI/TDSM electronic structures found in our calculations. For the appearance of the TI case (Figure 2a), a p<sub>z</sub>-like  $\Delta_7$  state needs to be pushed to the upper-most state of the valence p-band, thus a small c/a ratio is preferred for raising the  $p_z$  states up relative to the  $p_{x,y}$  states. Furthermore, strong coupling between B-X layers conducted by intercalated A atoms can split the  $p_z$  states into two branches, pushing one branch up. The coupling between B-X layers is determined not only by the c lattice constant but also by the c/a ratio, as

Journal of the American Chemical Society



**Figure 4.** Electronic structures of the predicted TIs in the lowest-energy structures from DFT+SOC. (a) Orbital-projected band structure of NaCaBi in the honeycomb (S1) structure (see Figure S2 in the Supporting Information for the band-inverted electronic structure of NaCaBi from HSE06<sup>23</sup>); (b) KBaBi (S1); (c) NaSrBi in the S2 structure (see Figure 3b); (d) NaBaBi (S2). The dotted lines with different colors denote the band projection onto different atomic orbitals. The band inversion is denoted in the figure by BI, with arrows pointing to the inverted states.

the A atom has equal distance nearest B and X neighbors only for small c/a ratio. Therefore, the predicted TIs are mainly distributed in the region with small c and small c/a ratio (see Figure 1c,d), with only two exceptions (CsCaN and CsCaBi) that have a very large A atom (Cs) and thus expanded c lattice constant (see Figure S5 in the Supporting Information for their band structures).

It is interesting to find that all ABX TIs (TDSMs) have the B atom from columns I (Na) and II (Ca) [XI (Cu) and XII (Zn)] in the periodic table with electronic configuration [ . . .]s<sup>n</sup> ([ . . .]d<sup>10</sup>s<sup>n</sup>), with the exceptions for the B = Mg (group II) (see their band structures in Figure S4 of the Supporting Information). These trends and exceptions are quite understandable from the view of elemental sizes as Mg has similar atomic/ionic sizes as the B from XII and XI but much smaller atomic/ionic sizes than the other II and I species (Ca, Sr, Ba, Li, Na, K, Rb, Cs). Furthermore, the strong hybridization between B-d and X-p valence states for B elements with [ . . .]d<sup>10</sup>s<sup>n</sup> electronic shells (see, e.g., Figure S6 in the Supporting Information for the case of LiAuTe) could decrease the B–X distance, leading to large c/a ratio and smaller coupling between B–X layers thus preference for TDSM.

**2.3.** Co-evaluation of Stability and Tl-ness: The ABX Bismides as Novel Tls. 2.3.1. Stable ABX Compounds That Are Tls. We will next focus on ABX compounds that are both TI and stable. This inquiry is motivated by the recent recognition<sup>29</sup> that band inversion—that is, population of antibonding conduction states and depopulation of bonding valence states—while promoting topological character can also thermodynamically destabilize the compound if it such inversion occurs in a significant fraction of the Brillouin zone in compounds unable to strongly screen the ensuing atomic

displacements (such as ionic oxides<sup>29</sup>). Thus, one must examine if the predicted structures are stable dynamically<sup>30,31</sup> and whether a structure is stable against decomposition into competing phases<sup>32</sup> (see Figure S7 in the Supporting Information for the case of NaCaBi).

The compounds and structures indicated in Figure 3 in red are predicted to be TI, whereas black indicates normal insulators. From the examination of the above-noted thermodynamic stability, we identify two ABX compounds, NaCaBi and KBaBi, that are stable in the honeycomb structure. Furthermore, we identify another seven compounds I-II-Bi (with I = Na, K Rb; II = Ca, Sr, Ba) that are thermodynamically stable in other structures (denoted S2-S5 in Figure 3) against disproportionation in their competing phases. In addition to the honeycomb-stable TIs NaCaBi and KBaBi, we find another two compounds, NaSrBi and NaBaBi, are stable in the S2 structure and predicted to be TIs from DFT+SOC (NaBaBi in a slightly higher-energy structure S3 was predicted to be TI before<sup>33</sup>). Figure 4 shows the electronic structures of the predicted TIs in the lowest-energy structures, with blue arrows indicating their band inversions. Their (inversion energies, fundamental band gaps) are (0.89, 0.34) eV for NaCaBi (S1), (0.33, 0.22) eV for KBaBi (S1), (0.20, 0.05) eV for NaSrBi (S2), and (0.05, 0.05) eV for NaBaBi (S2). In addition to the k-path adopted in Figure 4a,b and Figures S2 and S3 in the Supporting Information for honeycomb TIs and TDSMs, we checked another k-path  $(\Gamma - M - K - \Gamma - A - L - H - A)$  for all the 816 ABX honeycombs (see, e.g., Figures S4 and S5 in the Supporting Information). The above two *k*-paths include all the high symmetry *k*-lines in the Brillouin zone of honeycomb (S1) structure. In the predicted honeycomb topological materials, we did not find any Dirac points away from  $\Gamma$ -A k-line where the  $C_3$  rotation symmetry can protect the four-fold Dirac point. As all of the predicted TDSMs are in the centrosymmetric honeycomb structure, the two-fold Weyl nodes (band crossing by two singly degenerated bands at arbitrary k-points) do not exist. Figure 3 also shows that all the ABX compounds stable in S4 and S5 structures are normal insulators. We next attempted to understand this trend based on the structural features of this subgroup of ABX compounds.

2.3.2. TI-Enabling Structural Motif for Stable ABX Bismide 71. The S1 (honeycomb), S2, and S3 structures that are TIs have a similar structure motif, BiA<sub>6</sub>B<sub>3</sub> (or analogously BiB<sub>6</sub>A<sub>3</sub>), that is, Bi surrounded by an A<sub>6</sub> triangular prism and intercalated with a B3 triangle, as shown in Figure 1 and Figure 3, whereas this motif is missing in S4 and S5 structures that are stable but not TIs. We have calculated the properties of these five structures considering ABX and permutated BAX configurations for the nine compounds with DFT+SOC and systematically found the same situation as above; that is, all structures without BiA<sub>6</sub>B<sub>3</sub> motif (S4, S5) are normal insulators, whereas all structures with the BiA<sub>6</sub>B<sub>3</sub> motif (S1, S2, S3) are TIs. There is but a very weak exception (KBaBi in S3 structure with a band gap of 14 meV from DFT+SOC; see Figure S8 in the Supporting Information).

We have seen that the size factor (Figure 1) as represented by a, c/a in honeycomb structure, especially the size of the B atom (e.g., Mg and Zn versus Ca and Sr), is related to the selectivity within the ABX honeycomb lattice to TI versus TDSM in band-inverted ABX. We further note that the splitting of the pz states due to interlayer coupling can push one  $p_z$  state up to valence band maximum (VBM). The underlying factor is the anisotropic size of the local motifs (XA<sub>6</sub>B<sub>3</sub>; see Figure 1b and Figure 3b) in the periodic structure that can also affect the band inversion; for example, if the interlayer coupling is reduced, the VBM pz state moves down, and the band inversion could be removed. The conduction band minimum (CBM) s state will also be affected by the size of the local motif. The high coordination number of Bi surrounded by positively charged ions in the large-sized BiA<sub>6</sub>B<sub>3</sub> motif helps delocalize the CBM Bi-s state toward cations and shift the Bi-s level down (the relativistic Mass-Darwin effects also shift down the Bi-s level). Furthermore, the highly symmetrized structure of the XA<sub>6</sub>B<sub>3</sub> motif increases state repulsions shifting VBM (CBM) up (down) and thus helps form band inversions, analogous to the highly symmetrical BO<sub>6</sub> motif in ABO<sub>3</sub> TIs.<sup>29</sup> In Figure 3, we see a TI to narrow-gap (~14 meV) normal insulator transition along with the cation substitution from KCaBi to KBaBi, which could be related to the variation of the motif sizes and shapes due to cation variations.

2.3.3. Pressure-Stabilized Honeycomb Bismide Tl. Similar to the BiA<sub>6</sub>B<sub>3</sub> motifs discussed above, in ref 29, a BO<sub>6</sub> motif was found to be responsible for the band inversion in ABO<sub>3</sub> TIs. Furthermore, it is found that large enough distortions to the BO6 motif can remove the band inversion, and once the distortions are *partially* or fully restored (e.g., by external pressure), the band inversion could be recovered.<sup>29</sup> Many ABX compounds predicted to be TIs in the honeycomb structure in Figure 3a are stable in non-honeycomb structures at ambient conditions (similarly for the many topological materials in Figure 1c), such as RbBaBi with lowest-energy structure S5 (Pnma; see Figure 3b), which is an antiferroelectrically distorted version of S1 (honeycomb) structure. 34,35 We

consider the possibility of restoring the antiferroelectric distortion and thus stabilizing the honeycomb TI structures by pressure. As an example, we apply hydrostatic pressure to RbBaBi that is a normal insulator at ambient condition in its ground state structure (Pnma; see Figure 3b) and find that a 0.1 GPa pressure on RbBaBi can induce a transition from the Pnma structure to the honeycomb structure, as shown in Figure 5a. Figure 5b shows that the stable honeycomb RbBaBi

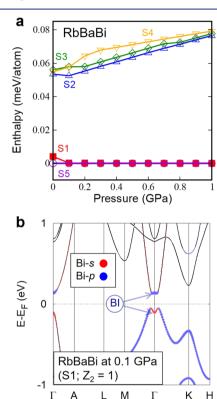


Figure 5. Pressure-stabilized TI phase in RbBaBi. (a) Enthalpy of crystal structures (shown in Figure 1 and Figure 3) of RbBaBi under hydrostatic pressure. We chose the lower-energy from ABX and BAX (for cation swapping) configurations. (b) Electronic structure of honeycomb (S1) RbBaBi under pressure of 0.1 GPa from DFT+SOC. The dotted lines with different colors denote the band projection onto different atomic orbitals. The band inversion is denoted by BI, with arrows pointing to the inverted states.

at 0.1 GPa is a TI, indicating that a rather small decrease of lattice volume by the external pressure (comparable to the variation of relaxed volumes from generalized gradient approximation to local density approximation 36,37 to DFT, as applied in ref 35) can remove the antiferroelectric distortion and stabilize the TI phase. This result suggests that once the TI-enabling structural motif is identified, one can design external constraints to achieve such structural motif and the related TI phase.

## 3. CONCLUSIONS

We found from DFT calculations 256 new topological materials in the family of ABX honeycomb compounds and distilled an interesting chemical rule to separate them into TIs and TDSMs simply by the identity of the B species in the formula. The chemical rule is based on the analysis of the double group representations of the band edge states in the honeycomb  $(P6_3/mmc)$  lattice that are determined by the interplay between ionic sizes and atomic orbitals in the local structures (i.e.,  $X[B_3A_6]$ ) associated with topological properties. The simple chemical regularity shed light on the high-throughput design of complicated and subtle material functionalities (e.g., the TDSM versus TI that requires detailed analysis of irreducible representations of the states near Fermi level); that is, instead of performing elaborate studies of each structure, the chemical rule distilled from a set of materials can be used to guide fast assignment of functional materials based on their chemical formulas, followed by verification on representative cases.

The special local motif,  $X[B_3A_6]$ , was found to coincide with the appearance of topological band inversion in various structure types of the I-II-Bi group of materials; that is, structures with (without) such a motif are TI (NI) with a negligible exception case. For a structure without such a motif and thus not TI, we applied external pressure to reinforce the needed structural motif and achieved a TI phase at a pressure of 0.1 GPa. The functionality-enabling structural motif and the possibility to realize it in materials where it does not appear naturally open the way of target-oriented design of functional materials. Instead of finding a special functionality from the variety of structure motifs by accident, we can first identify the functionality-enabling structural motifs via rational study of structures that are not necessarily stable at ambient conditions and then use these special motifs to construct potential functional materials, followed by stability test or design of external constraints to stabilize the designed materials.

#### 4. THEORETICAL METHODS

The structural parameters were determined by DFT total energy minimization. Total energies were calculated using the projectoraugmented wave (PAW) pseudopotential<sup>38</sup> total energy method without spin-orbit coupling with the GGA approximation to DFT and the exchange-correlation of Perdew-Burke-Ernzerhof (PBE)<sup>39</sup> as implemented in the Vienna ab initio simulation package (VASP).40 We use an energy-cutoff of 520 eV and reciprocal space grids with densities of  $2\pi \times 0.068 \text{ Å}^{-1}$  and  $2\pi \times 0.051 \text{ Å}^{-1}$  for relaxation and static calculation, respectively. Electronic structure and physical properties were calculated from DFT taking into account spin-orbit coupling (SOC) by a perturbation to the pseudopotential<sup>41</sup> (is the angular momentum eigenstate of atomic site i). To illustrate the band inversions, we project the calculated wave function on spin and orbital basis of each atomic site and then sum for a given atomic orbital. The Wigner-Seitz radii for constructing used in this study are listed in the pseudopotentials of the VASP simulation package.<sup>40</sup> The surface states were calculated by the effective tight-binding Hamiltonians of a freestanding thick slab consisting of 20 unit-cells along (001) direction. The hopping parameters were generated from maximally localized Wannier function (MLWF),<sup>42</sup> which is constructed from self-consistent DFT calculations of bulk materials. With the MLWF hopping parameters, an iterative method<sup>43</sup> implemented in WannierTools<sup>44</sup> is used to obtain the surface Green's function of the thick slab.

### ASSOCIATED CONTENT

## Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/jacs.8b06652.

Full list of studied ABX honeycomb structures, theoretical methods, additional figures and tables on the properties of ABX topological materials (PDF)

#### AUTHOR INFORMATION

#### **Corresponding Authors**

\*xiuwenzhang@szu.edu.cn

\*alex.zunger@colorado.edu

#### ORCID 0

Xiuwen Zhang: 0000-0003-1003-2885 Qihang Liu: 0000-0001-9843-2482

#### **Present Address**

<sup>V</sup>Q.L.: Department of Physics and Shenzhen Institute for Quantum Science and Technology, Southern University of Science and Technology, Shenzhen 518055, China.

# **Author Contributions**

X.Z., Q.L., and Q.X. contributed equally to this work.

#### Notes

The authors declare no competing financial interest.

#### ACKNOWLEDGMENTS

The work of A.Z., Q.L., and X.Z. was supported by Department of Energy, Office of Science, Basic Energy Science, MSE division under Grant No. DE-FG02-13ER46959 to CU Boulder. This research used resources of the National Energy Research Scientific Computing Center (NERSC), a U.S. Department of Energy Office of Science User Facility operated under Contract No. DE-AC02-05CH11231. The work of X.Z. in China was supported by National Natural Science Foundations of China (Grant No. 11774239), National Key R&D Program of China (Grant No. 2016YFB0700700), and Shenzhen Science and Technology Innovation Commission (Grant Nos. ZDSYS201707271554071, JCYJ20170412110137562, JCYJ20170818093035338).

# ■ REFERENCES

- (1) Hasan, M. Z.; Kane, C. L. Rev. Mod. Phys. 2010, 82, 3045.
- (2) Qi, X.-L.; Zhang, S.-C. Rev. Mod. Phys. 2011, 83, 1057.
- (3) Kane, C. L.; Mele, E. J. Phys. Rev. Lett. 2005, 95, 146802.
- (4) Bernevig, B. A.; Hughes, T. L.; Zhang, S.-C. Science 2006, 314, 1757.
- (5) Wang, Z.; Sun, Y.; Chen, X.-Q.; Franchini, C.; Xu, G.; Weng, H.; Dai, X.; Fang, Z. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2012**, 85, 195320.
- (6) Liu, Z. K.; Zhou, B.; Zhang, Y.; Wang, Z. J.; Weng, H. M.; Prabhakaran, D.; Mo, S.-K.; Shen, Z. X.; Fang, Z.; Dai, X.; Hussain, Z.; Chen, Y. L. *Science* **2014**, *343*, 864.
- (7) Zhang, H. J.; Liu, C.-X.; Qi, X.-L.; Dai, X.; Fang, Z.; Zhang, S.-C. *Nat. Phys.* **2009**, *5*, 438.
- (8) Gu, Z.-C.; Wen, X.-G. Phys. Rev. B: Condens. Matter Mater. Phys. 2009, 80, 155131.
- (9) Yang, B.-J.; Nagaosa, N. Nat. Commun. 2014, 5, 4898.
- (10) Wu, Q.-S.; Piveteau, C.; Song, Z.; Yazyev, O. V. MgTa<sub>2</sub>N<sub>3</sub>: A reference Dirac semimetal. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2018**, 98, 081115.
- (11) Young, S. M.; Zaheer, S.; Teo, J. C. Y.; Kane, C. L.; Mele, E. J.; Rappe, A. M. *Phys. Rev. Lett.* **2012**, *108*, 140405.
- (12) Liang, T.; Gibson, Q.; Ali, M. N.; Liu, M.; Cava, R. J.; Ong, N. P. Nat. Mater. 2015, 14, 280.
- (13) Zhang, H. J.; Chadov, S.; Müchler, L.; Yan, B.; Qi, X. L.; Kübler, J.; Zhang, S. C.; Felser, C. *Phys. Rev. Lett.* **2011**, *106*, 156402.
- (14) Gibson, Q. D.; Schoop, L. M.; Muechler, L.; Xie, L. S.; Hirschberger, M.; Ong, N. P.; Car, R.; Cava, R. J. Phys. Rev. B: Condens. Matter Mater. Phys. 2015, 91, 205128.
- (15) Du, Y.; Wan, B.; Wang, D.; Sheng, L.; Duan, C.-G.; Wan, X. Sci. Rep. 2015, S, 14423.

- (16) Zhang, X.; Liu, Q.; Luo, J. W.; Freeman, A. J.; Zunger, A. Nat. Phys. **2014**, 10, 387.
- (17) Wang, Z.; Alexandradinata, A.; Cava, R. J.; Bernevig, B. A. *Nature* **2016**, 532, 189.
- (18) Kohn, W.; Sham, L. J. Phys. Rev. 1965, 140, 1133.
- (19) Kresse, G.; Joubert, D. Phys. Rev. B: Condens. Matter Mater. Phys. 1999, 59, 1758.
- (20) Perdew, J. P.; Burke, K.; Ernzerhof, M. Phys. Rev. Lett. 1996, 77, 3865.
- (21) Kresse, G.; Furthmüller, J. Comput. Mater. Sci. 1996, 6, 15.
- (22) Heyd, J.; Scuseria, G. E.; Ernzerhof, M. J. Chem. Phys. 2003, 118, 8207.
- (23) Heyd, J.; Scuseria, G. E.; Ernzerhof, M. J. Chem. Phys. 2006, 124, 219906.
- (24) Fu, L.; Kane, C. L.; Mele, E. J. Phys. Rev. Lett. 2007, 98, 106803.
- (25) Fu, L.; Kane, C. L. Phys. Rev. B: Condens. Matter Mater. Phys. 2006, 74, 195312.
- (26) Yu, R.; Qi, X. L.; Bernevig, A.; Fang, Z.; Dai, X. Phys. Rev. B: Condens. Matter Mater. Phys. 2011, 84, 075119.
- (27) Fu, L.; Kane, C. L. Phys. Rev. B: Condens. Matter Mater. Phys. 2007, 76, 045302.
- (28) Liu, Q.; Zunger, A. Phys. Rev. X 2017, 7, 021019.
- (29) Zhang, X.; Abdalla, L. B.; Liu, Q.; Zunger, A. Adv. Funct. Mater. 2017, 27, 1701266.
- (30) Gautier, R.; Zhang, X.; Hu, L.; Yu, L.; Lin, Y.; Sunde, T. O. L.; Chon, D.; Poeppelmeier, K. R.; Zunger, A. Nat. Chem. 2015, 7, 308.
- (31) Zhang, X.; Yu, L.; Zakutayev, A.; Zunger, A. Adv. Funct. Mater. 2012, 22, 1425.
- (32) Inorganic Crystal Structure Database; Fachinformationszentrum Karlsruhe, Germany, 2006.
- (33) Sun, Y.; Wang, Q.-Z.; Wu, S.-C.; Felser, C.; Liu, C.-X.; Yan, B. Phys. Rev. B: Condens. Matter Mater. Phys. 2016, 93, 205303.
- (34) Bennett, J. W.; Garrity, K. F.; Rabe, K. M.; Vanderbilt, D. *Phys. Rev. Lett.* **2013**, *110*, 017603.
- (35) Monserrat, B.; Bennett, J. W.; Rabe, K. M.; Vanderbilt, D. *Phys. Rev. Lett.* **2017**, *119*, 036802.
- (36) Zunger, A.; Perdew, J. P.; Oliver, G. L. Solid State Commun. 1980, 34, 933.
- (37) Perdew, J. P.; Zunger, A. Phys. Rev. B: Condens. Matter Mater. Phys. 1981, 23, 5048.
- (38) Kresse, G.; Joubert, D. Phys. Rev. B: Condens. Matter Mater. Phys. 1999, 59, 1758.
- (39) Perdew, J. P.; Burke, K.; Ernzerhof, M. Phys. Rev. Lett. 1996, 77, 3865.
- (40) Kresse, G.; Furthmüller, J. Comput. Mater. Sci. 1996, 6, 15.
- (41) Błoński, B.; Hafner, J. Phys. Rev. B: Condens. Matter Mater. Phys. 2009, 79, 224418.
- (42) Marzari, N.; Mostofi, A. A.; Yates, J. R.; Souza, D.; Vanderbilt, D. Rev. Mod. Phys. **2012**, 84, 1419.
- (43) Sancho, M. P. L.; Sancho, J. M. L.; Rubio, J. J. Phys. F: Met. Phys. 1985, 15, 851.
- (44) Wu, Q.; Zhang, S.; Song, H.-F.; Troyer, M.; Soluyanov, A. A. Comput. Phys. Commun. 2018, 224, 405.